GLOBAL JOURNAL OF ENGINEERING SCIENCE AND RESEARCHES

ITERATIVE LOW PASS FILTER RECONSTRUCTION OF CONVOLUTION IMAGES USING MULTI-RESOLUTION APPROXIMATIONS

Tohid Aribi
Department of Electrical Engineering, Miandoab Branch, Islamic Azad University, Miandoab, Iran
tohidaribi@gmail.com

ABSTRACT

In this letter, the two wavelet families, biorthogonal and Riesz bases are introduced. Biorthogonality for two possible decompositions in these bases, The Riesz stability implies that there exist such that Biorthogonal wavelet bases are related to multiresolution approximations. The direct consequence of the above derivation is tradeoff made between the support size of a wavelet and its number of vanishing moment. The goal is family Riesz basis of the space it generates, whereas a Riesz respectively can verify that are two multiresolution approximations. The dilated and The Biorthogonality of the decomposition and reconstruction wavelets implies that is not orthogonal to, whereas signal is not orthogonal which is proven in this article.

Keywords: Biorthogonal, Riesz bases, Bezout, Daubechies, wavelet etc.

I. INTRODUCTION

One cannot have a wavelet of compact support with an arbitrary high vanishing moments [1-2]. To ensure a wavelet with vanishing moments has a minimal support, we need construct a minimum degree. The difficulty is to design a polynomial of minimum degree such that since is real, is an even function and thus can be written as a polynomial and we can also quadrature condition is equivalent to for any. To minimize the nonzero terms of the finite Fourier series we must find the solution of minimum degree, which is obtained with the Bezout [3-5] classical theorem on polynomials. The Bezout theorem proves that there exist two unique polynomials possible factorizations, the minimum phase solution is obtained by choosing to be inside the unit circle. The resulting causal filter is a Daubechies filter. If a wavelet with vanishing moments that generates an orthonormal basis, then it has a support size larger or equal [6-7]. A Daubechies wavelet calculated with Daubechies filter banks has a minimum size of support equal to. The support of the corresponding scaling functions is as an example, Daubechies scaling functions and wavelet at scale vanishing moments respectively [4-5]. Daubechies wavelets are very asymmetric because they are constructed by selecting the minimum phase square root. One can show that filters corresponding to a minimum phase square root have their energy optimally concentrated near the starting point of their support. They are thus highly non-symmetric, which yields very asymmetric wavelets. To obtain symmetric or anti-symmetric wavelet, the filter must be Symmetric or anti-symmetric with respect to the center of its support, which means that has a linear phase.

II. METHODS AND MATERIALS

Haar filter is the only real compactly supported conjugate mirror filter that has a linear phase. The filters of Daubechies are obtained by optimizing the choice of the square root to obtain an almost linear phase. The resulting wavelet still have a minimum support with vanishing moments but they are more symmetric. A fast wavelet transform decomposes successively each approximation into a coarser resolution plus the wavelet coefficients. Figure 1, a framework for multi-scale fusion with wavelet transform. The filter removes the higher frequencies of the inner product sequence a whereas is a high-pass filter which collects the remaining highest frequencies. The reconstruction is an interpolation that inserts zeros to expand and filter these signals. A fast wavelet transform is computed with a cascade of filters with hand followed by a factor 2 subsampling. A fast inverse wavelet transform reconstructs progressively each a by inserting zeros between samples of filtering and adding the outputs. The decomposition of a discrete signal in conjugate mirror filters can be interpreted as an expansion in a basis, the resulting family an orthogonal basis. An orthogonal wavelet representation is composed of wavelet coefficients of scales plus the remaining approximation at the largest scale. It is computed by iterating numerical example computed with the Daubechies filter. The original signal a is recovered from this wavelet representation by iterating the reconstruction. The conjugate mirror filters are often used in filter banks that cascade several levels of filtering and subsampling. It is thus necessary to understand the behavior of such a cascade. In a wavelet filter bank tree, the output of the low-pass filter h is sub or conjugate mirror filters, one can verify that this family is an orthonormal basis. These discrete vectors are close to a uniform sampling of the continuous time scaling functions and wavelets. When the number of successive convolutions increases, one can verify that converges respectively. We therefore refer as a Discrete Wavelet Basis. The fast discrete wavelet transform decomposes signal into low-pass and high-pass components subsampled, the inverse transform performs the reconstruction. Study of such classical multirate filter banks became a major signal processing topic, when it discovered that it is possible to perform such decompositions and reconstructions with quadrature mirror filters. However, besides the simple Haar filter, a quadrature mirror filter cannot have a finite impulse response. It is found necessary and sufficient conditions for obtaining perfect reconstruction orthogonal filters with a finite impulse response, that they called conjugate mirror filters.

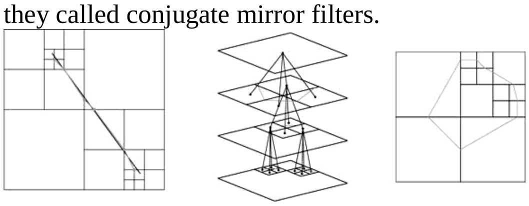

Figure 1, multi-scale fusion with wavelet transform

III. RESULTS

The theory was completed by the biorthogonal mirror filter equations. We follow this digital signal processing approach which gives a simple understanding of perfect reconstruction filter banks. A two-channel multirate filter bank convolves a signal with a low-pass filter a high-pass filter and subsamples the output. The factor gain which is inverse for the decomposition and reconstruction filters and is a reverse shift. We generally set the internal relationship between biorthogonal filter banks become in the time domain, can be written as the two pairs of filters plays a symmetric role and can be inverted. The biorthogonal condition simplifies to If we impose that the decomposition filter is equal to the reconstruction filter is exactly the condition of conjugate mirror filters given in Equation proves, with some additional conditions, and are the Fourier transforms of finite energy functions. The support size, the number of vanishing moments, the regularity and the symmetry of biorthogonal wavelets is controlled with an appropriate design of hand. Similar to the case of orthogonal wavelets, one can show that is nonzero respectively for a support equal. Notice that the support and are respectively. Both wavelets thus have the same size of support, which show that the number of vanishing moments. They depends on the number of zeros for conclude that has vanishing moments if and only if has a zero of order whereas, has vanishing moments if and only has a zero. On the other hand, the smoothness and can be related to the order of zeros. This is intuitively make sense by the more number of zeros, the smoother. Vanishing moments and the regularity of biorthogonal wavelet are biorthogonal scaling functions and wavelets generated. It increases, which is the vanishing moments of, similarly, the regulari. Perfect reconstruction filters for compactly supported spline biorthogonal wavelets with vanishing moments. To produce small wavelet coefficients in the regular regions, we must compute the inner products using the wavelet with the maximum number of vanishing moments. The reconstructions is then performed with the other wavelet, which is generally the smoother one. It is possible to construct smooth biorthogonal wavelets of compact support which are either symmetric or antisymmetric. This is impossible for orthogonal wavelets, except the particular case of the Haar basis.
Symmetric or antisymmetric wavelets are synthesized with perfect reconstruction filters having a linear phase. This flexibility results in more robust registration in the presence of noise. Maximization of the divergence is a very general criterion, because no assumptions are made in regards to the nature of this dependence and no limiting constraints are imposed on image contents. Simulation results demonstrate that our approach achieves an effective estimation of the target motion automatically without any prior feature extraction.

This is a desirable property for many applications. The biorthogonal wavelets with a minimum size of support are constructed with a technique introduced in [7], A new generalized divergence measure, is proposed. We prove the convexity of this divergence measure, derive its maximum value, and analyze its upper bounds in terms of the Bayes error in statistical pattern recognition. Based on the divergence, we propose a new approach to the problem of image registration. This is accomplished by using the divergence to measure the statistical dependence between consecutive image frames, which is maximal if the images are geometrically aligned, which is similar to the construction of Daubechies wavelets.

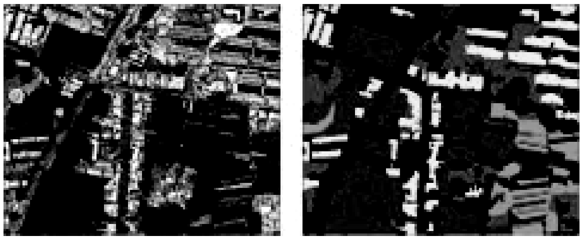

Figure 2 image fusion by wavelet based scheme.

As an example, it gives the coefficients of perfect reconstruction filters of compactly supported spline wavelets for symmetric and antisymmetric biorthogonal wavelets. A lifting is an elementary modification of perfect reconstruction filters, which is used to improve the wavelet properties. Compactly supported biorthogonal wavelet bases can be constructed from finite impulse response biorthogonal filters which satisfy the filter hand hare said to be dual. The following theorem [3] characterizes all filters of compact support that are dual. Filters with a finite support. A filter h with finite support is dual and only if there exists a finite filter such that This theory proves that if biorthogonal filters with The inverse Fourier transform gives and The new filters are said to be lifted because the use of lcan improve their properties. A new set of biorthogonal wavelet bases can be derived from the lifted filter banks [3]. Family of biorthogonal scaling functions and wavelets is defined by are biorthogonal wavelet bases. The lifting increases the support size typically by the length of the support. Design procedures compute minimum size filters lto achieve specific properties. It points out that the regularity number of vanishing is determined by the order of zeros. The coefficients of moments are often calculated to produce a lifted transfer function with more zeros.

IV. CONCLUSION

In the reverse direction, the reconstruction from wavelet coefficients recovers the following theorem shows that these coefficients are calculated with a cascade of discrete convolution and sub-sampling. At the reconstruction, it proves that are computed by taking every other sample of the convolution of with hand respectively. Divergence provides an ability to control the measurement sensitivity of the joint histogram.

V. REFERENCES

[1]. P.J. Burt and R. J. Kolczynski, "Enhanced image capture through fusion," Proc. 4th Intl Conference on Computer Vision, pp. 173–182, 2003.

[2]. Sedghi T., "A Fast and Effective Model for cyclic Analysis and its application in classification" Arabian Journal for Science and Engineering Vol. 38 October 2012.

[3]. Huntsberger T. L., Data fusion: A neural networks implementation, Data fusion in robotics and machine intelligence, M. Abidi and R. Gonzalez Eds., Academic Press, San Diego, 2012.

[4]. T. Sedghi, "Non Linear Transform for Retrieval System in Consideration of Feature Combination Technique" International Journal of Natural and Engineering Sciences, Vol 6 No 3, 2012.

[5]. Chen S., "Stochastic image algebra for multi-sensor fusion and spatial reasoning: a neural approach," Proc. SPIE, vol. 1098, pp. 146–154, 2009.

[6]. R. Luo and M. Kay, Data fusion and sensor integration: state of the art in 1990s, Data fusion in robotics and machine intelligence, M. Abidi and R. Gonzalez Eds., Academic Press, San Diego, 2012.

[7]. Wright W. A., "A markov random field approach to data fusion and color segmentation," Image Vision Comp., vol. 7, no. 2, pp. 144–150, 2009.